



Name: _____ () Class: _____ Date: _____

Overview

This worksheet covers the following:

1. Recognizing shape of quadratic functions
2. Sketching quadratic functions of the form $y = (x - h)^2 + k$ or $y = -(x - h)^2 + k$

Introduction

Previously in Chapter 2, we learned about quadratic equations – the 4 methods of solving them, and using them in word problems. Today, we are going to investigate more about quadratic equations – the different forms and shapes, how to describe them etc.

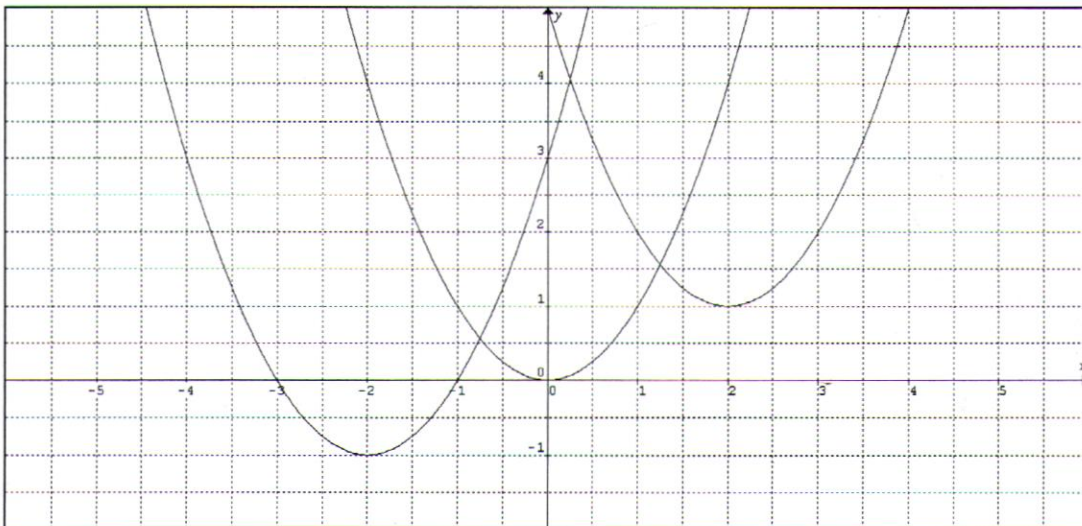
To begin, for any quadratic function $y = ax^2 + bx + c$

We can classify them into two types based on a (the coefficient of x^2):

1. a is +ve, or
2. a is -ve

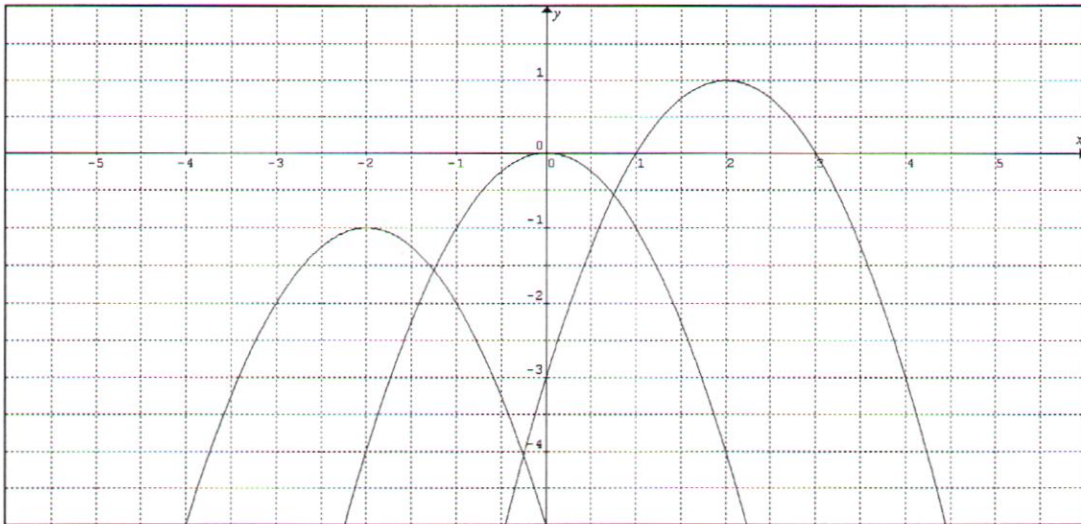
a is +ve

If a is +ve (e.g. $y = x^2, y = 2x^2 - 5x$), the quadratic functions will look like these:



a is -ve

If a is $-ve$ (e.g. $y = -x^2, y = -3x^2 + 2x - 1$), the quadratic functions will look like these:



What do you notice about their differences?

Complete the table below:

a is +ve ("Smiley Face") 😊	a is -ve ("Sad Face") ☹️
Shape of graph:	Shape of graph:
Graphs will have: <ul style="list-style-type: none">• <u>Minimum</u> point• Line of symmetry• Have a y-intercept• May or may not have x-intercepts	Graphs will have: <ul style="list-style-type: none">• <u>Maximum</u> point• Line of symmetry• Have a y-intercept• May or may not have x-intercepts

Question: Given a quadratic function, can we sketch the graph quickly and accurately?

To sketch a graph quickly and accurately, we can transform the quadratic function into one of these two forms (with their negative counterparts):

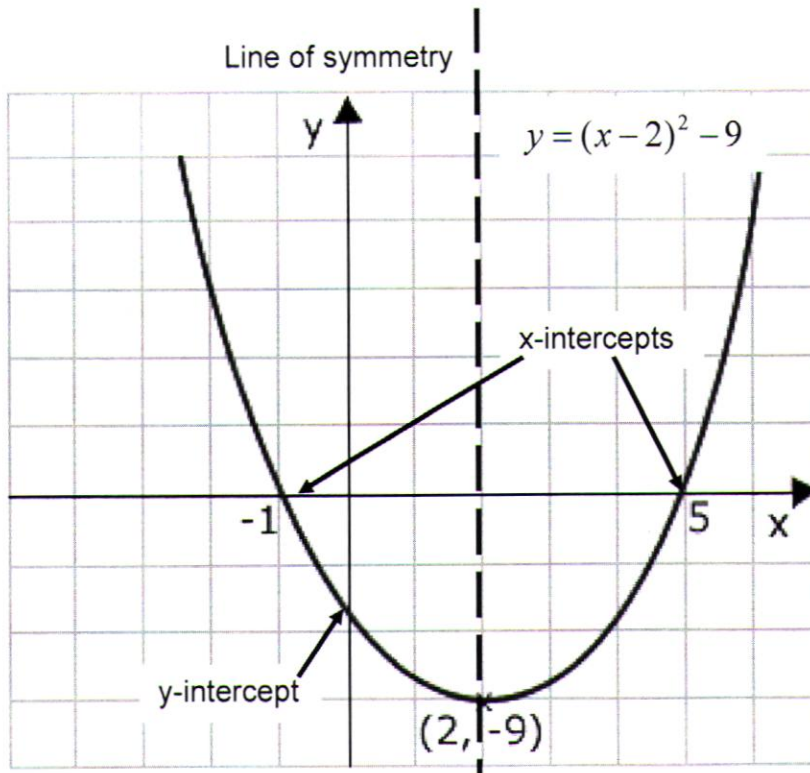
- | | | |
|-------------------------|----|-----------------------|
| 1. $y = (x - h)^2 + k$ | or | $y = -(x - h)^2 + k$ |
| 2. $y = (x - p)(x - q)$ | or | $y = -(x - p)(x - q)$ |

The difference between 1 and 2 is that the 2nd form means the graph has x-intercepts (i.e. it cuts the x-axis). Since this may not be true for all quadratic functions, not all quadratic functions can be expressed in the 2nd form.

Now let's investigate each of these forms closer.

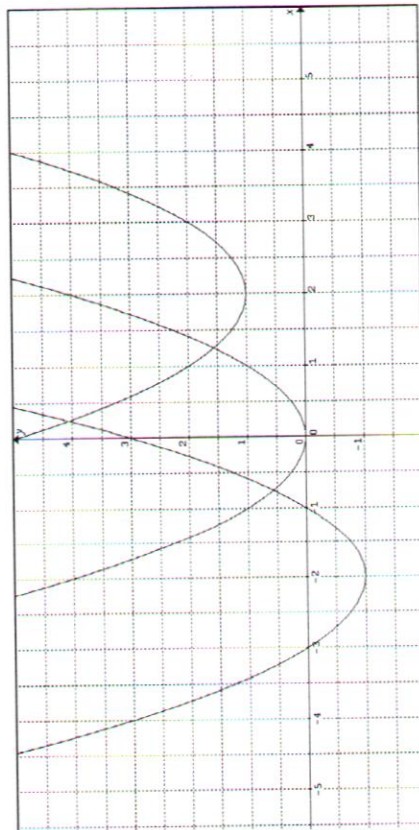
Example:

1. Smiley face or sad face? => Min or Max point? _____
2. Coordinates of min point _____
3. Line of symmetry? _____
4. y-intercept? _____



When a function is expressed as $y = (x - h)^2 + k$ or $y = -(x - h)^2 + k$, the graph will have a turning point at the point (h, k) . This turning point is either a minimum or maximum point depending on the coefficient of x^2 , i.e. a .

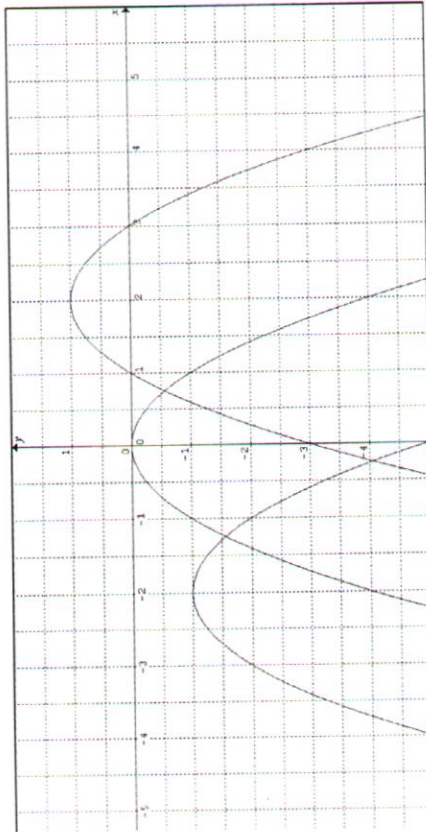
$$y = (x - h)^2 + k$$



Important points to note:

- "Smiley Face" – minimum point
- Turning/Min point at (h, k)
- Line of symmetry at $x = h$
- Label where it cuts the y-axis

$$y = -(x - h)^2 + k$$



Important points to note:

- "Sad Face" – maximum point
- Turning/Max point at (h, k)
- Line of symmetry at $x = h$
- Label where it cuts the y-axis

Example 1:

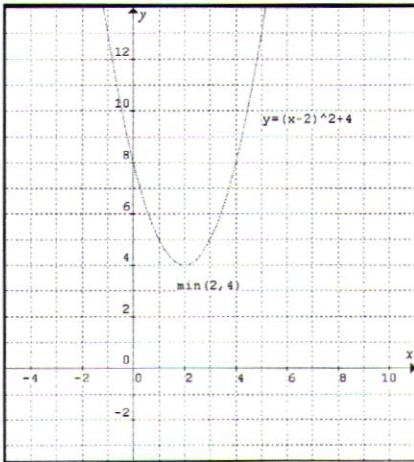
Sketch the graph of $y = (x-2)^2 + 4$

Steps:

5. Smiley face or sad face? => Min or Max point?
6. Coordinates of min point
7. Line of symmetry?
8. y-intercept?

$$\begin{array}{l} \text{min point} \\ \hline (2, 4) \\ \hline x = 2 \\ \hline y = 8 \\ \hline \end{array}$$

Once you have the above information, sketch the graph. Make sure you label the important information clearly.

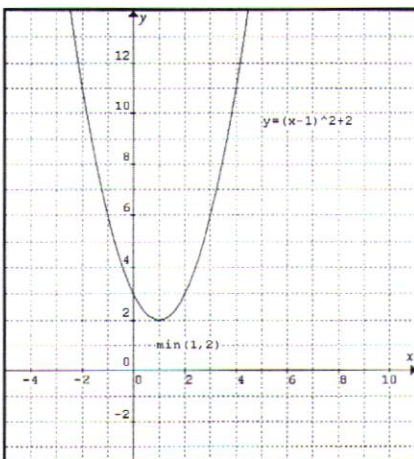


Example 2:

Sketch the graph of $y = (x-1)^2 + 2$

1. Smiley face or sad face? => Min or Max point?
2. Coordinates of min point
3. Line of symmetry?
4. y-intercept?

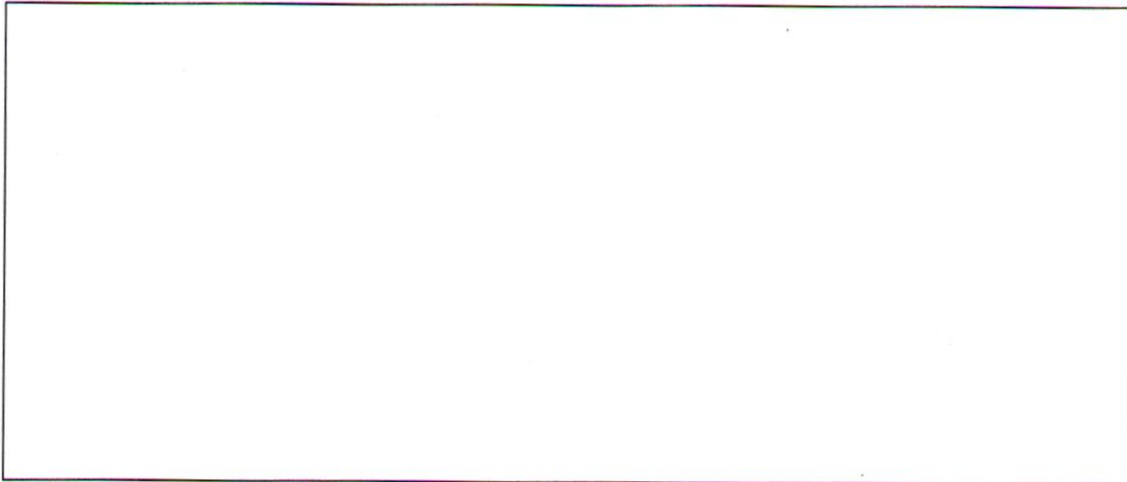
$$\begin{array}{l} \text{min point} \\ \hline (1, 2) \\ \hline x = 1 \\ \hline y = 3 \\ \hline \end{array}$$



Practice 1

Sketch the graph of $y = (x-1)^2 + 2$

1. Smiley face or sad face? => Min or Max point?
2. Coordinates of min point
3. Line of symmetry?
4. y-intercept?

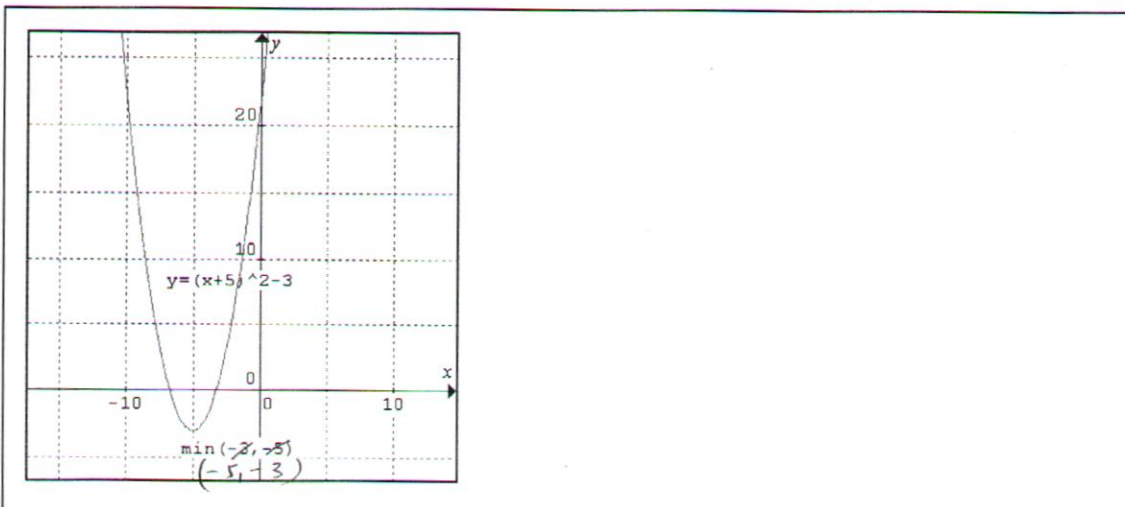


Practice 2

Sketch the graph of $y = (x+5)^2 - 3$

1. Smiley face or sad face? => Min or Max point?
2. Coordinates of turning point
3. Line of symmetry?
4. y-intercept?

min point
 $(-5, -3)$
 $x = -5$
 $y = -3$

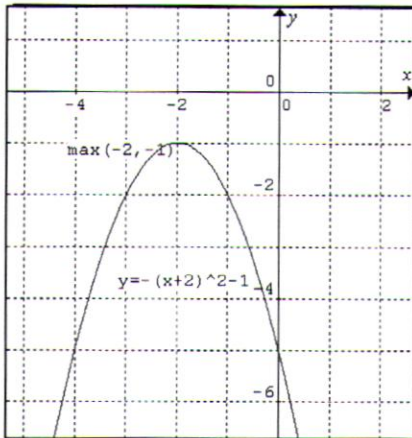


Example 3:

Sketch the graph of $y = -(x+2)^2 - 1$

1. Smiley face or sad face? => Min or Max point?
2. Coordinates of turning point
3. Line of symmetry?
4. y-intercept?
5. x-intercept?

max point
 $(-2, -1)$
 $x = -2$
 $y = -5$
no real roots

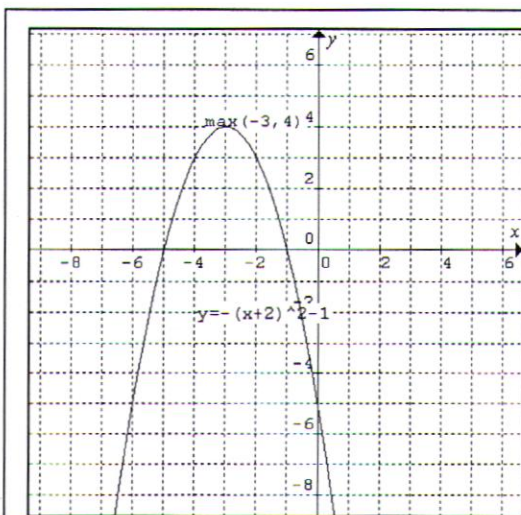


Practice 3:

Sketch the graph of $y = -(x+3)^2 + 4$

1. Smiley face or sad face? => Min or Max point?
2. Coordinates of turning point
3. Line of symmetry?
4. y-intercept?
5. x-intercept?

Max point
 $(-3, 4)$
 $x = -3$
 $y = -5$
 $x = -1$ or $x = -5$

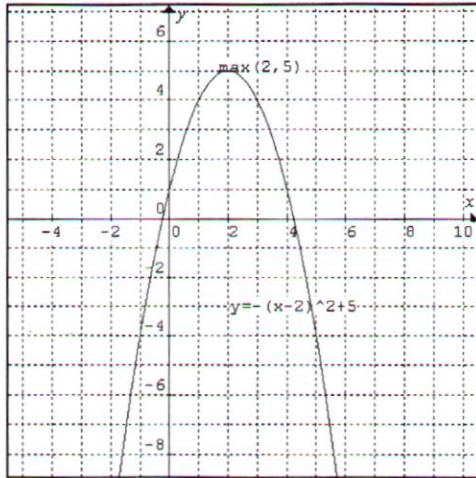


Practice 4

Sketch the graphs for the following quadratic equations, showing clearly:

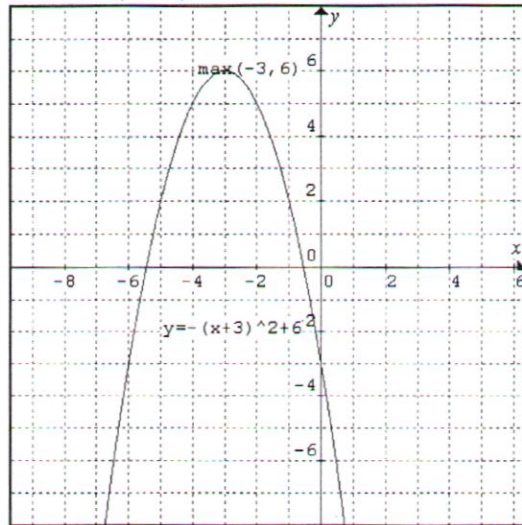
- min or max point
- line of symmetry (state the equation)
- y-intercept

a) $y = -(x-2)^2 + 5$



$$x = 4.24 \text{ or } x = -0.236$$

b) $y = -(x+3)^2 + 6$



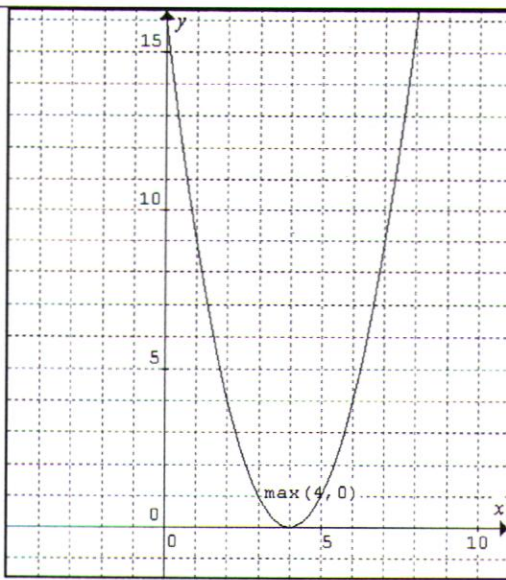
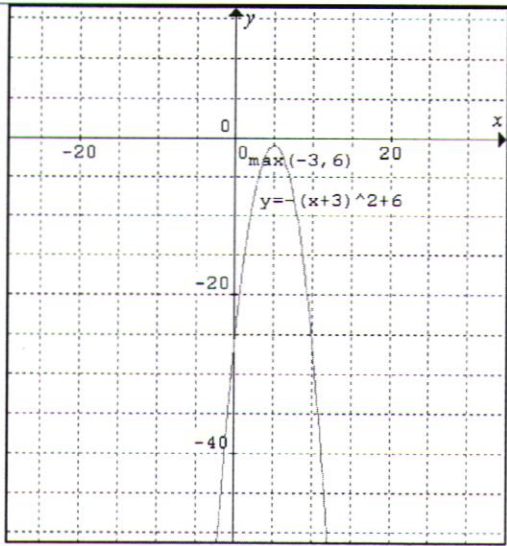
$$x = -0.551 \text{ or } x = -5.45$$

c) $y = -(x-5)^2 - 1$

x no real roots

d) $y = (x-4)^2$

$$x = 4$$

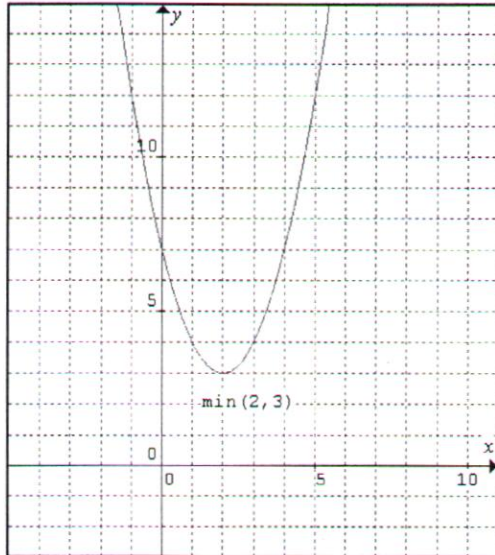


Homework

1. Sketch the graphs for the following quadratic equations, showing clearly:

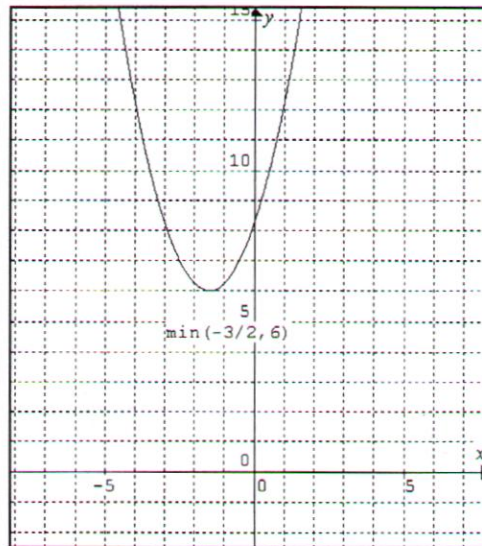
- min or max point
- line of symmetry (state the equation)
- y-intercept

a) $y = (x - 2)^2 + 3$



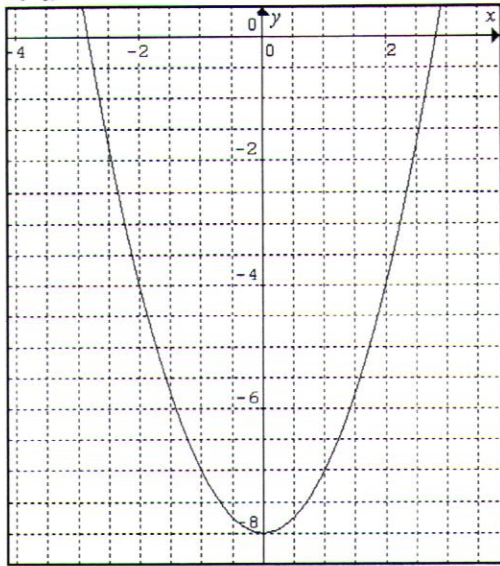
no real roots

b) $y = \left(x + \frac{3}{2}\right)^2 + 6$



no real roots

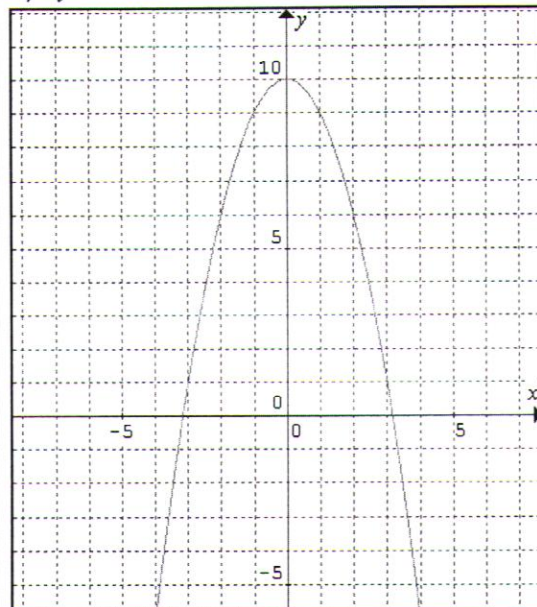
c) $y = x^2 - 8$



$\min(0, -8)$

$x = 2.83$ or $x = -2.83$

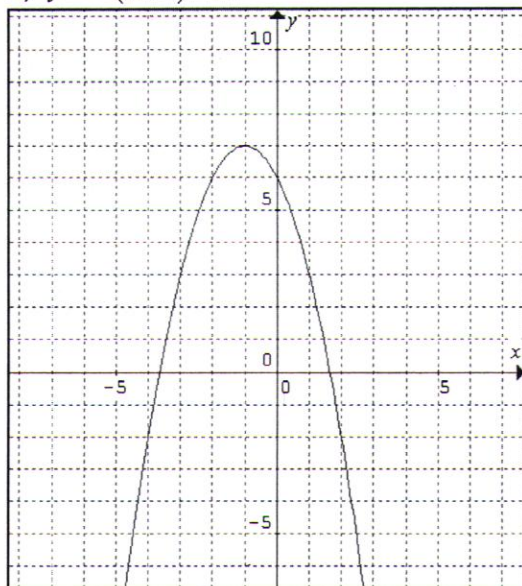
d) $y = -x^2 + 10$



$\max(0, 10)$

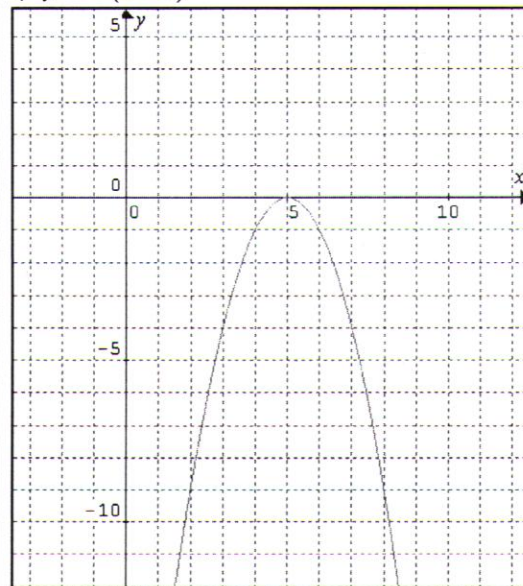
$x = 3.16$ or $x = -3.16$

e) $y = -(x+1)^2 + 7$



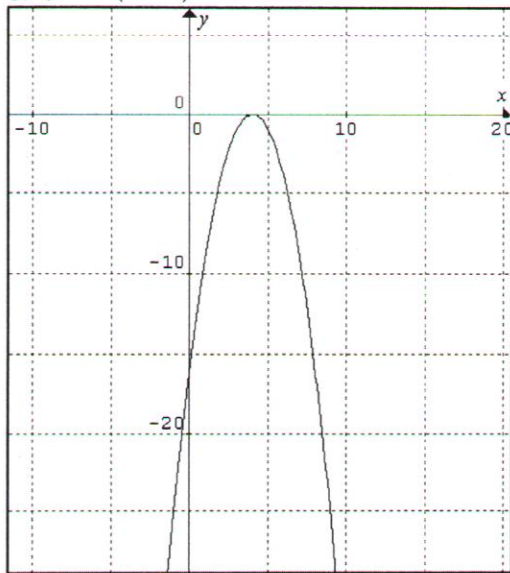
$x = 1.65$ or $x = -3.65$

f) $y = -(x-5)^2$



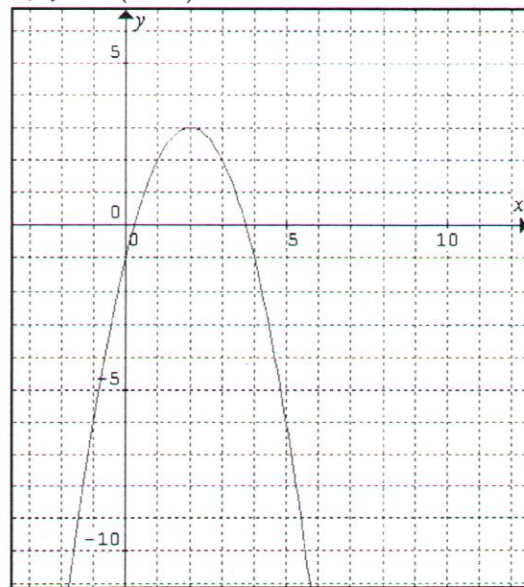
$x = 5$

g) $y = -(x-4)^2$



$x = 4$

h) $y = -(x-2)^2 + 3$



$x = 3.73$ or $x = 0.268$

Dateline: Mar 2011

My Reflection